



# Improving Ground Moving Target Indication Performance

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**MIT Lincoln Laboratory**



# GMTI Scenario

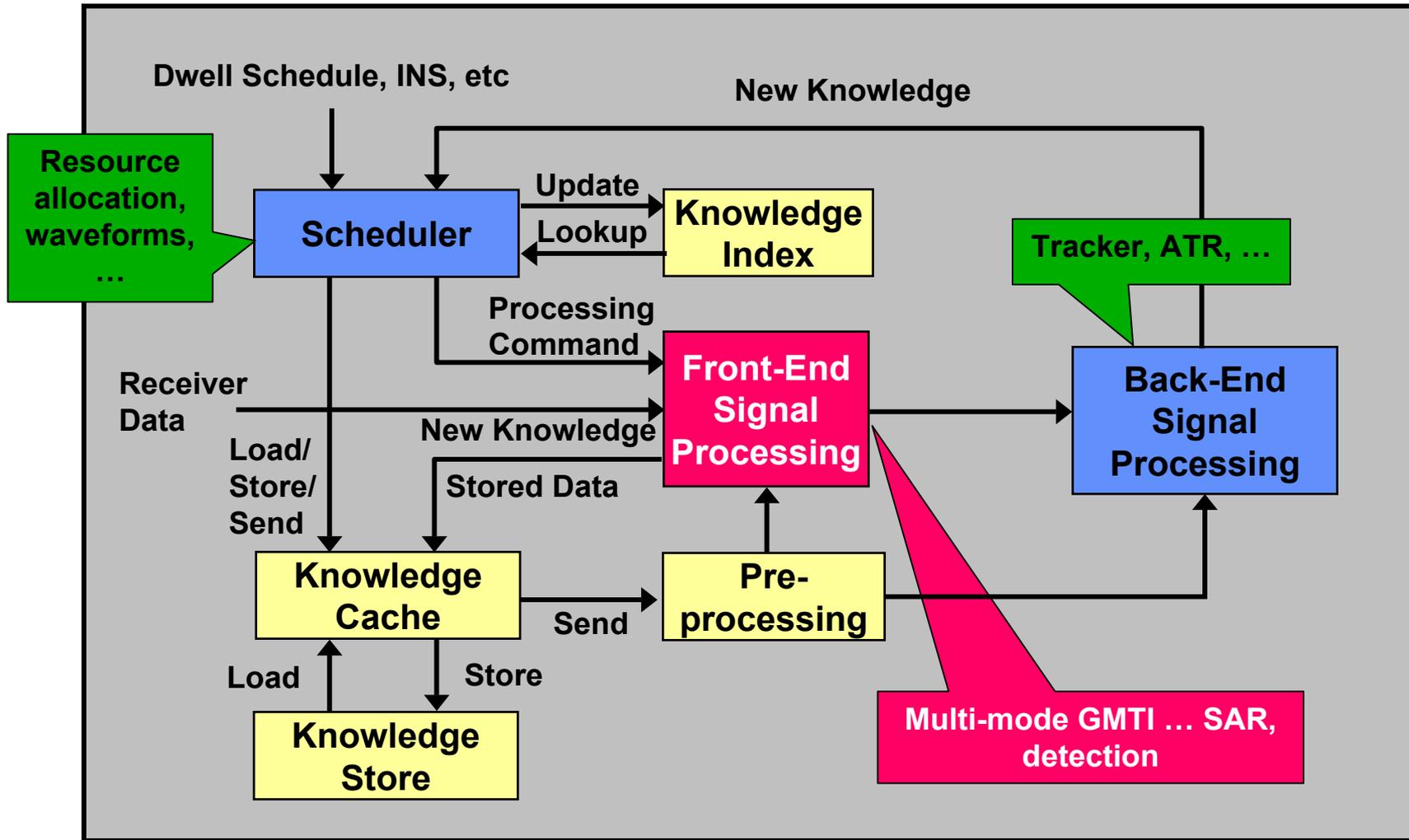


- GMTI/STAP CHALLENGES**
- Heterogeneous Clutter
  - Spiky Clutter
  - Dense Target Backgrounds
  - Low Doppler Targets

**KASSPER PROGRAM GOAL**  
Exploit a priori knowledge to address GMTI/STAP challenges in next generation ISR platforms



# KASSPER Processing Architecture



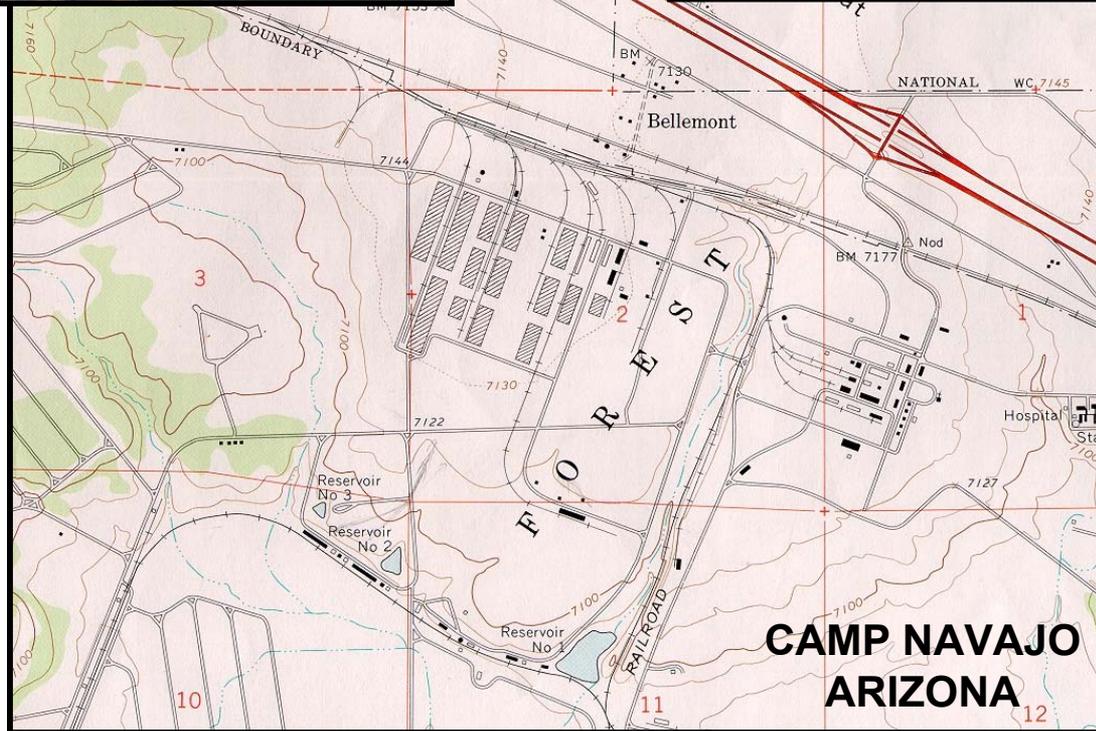
Focus of talk will explore several front-end signal processing techniques



# GMTI Scenario Example



## Tuxedo Sensor

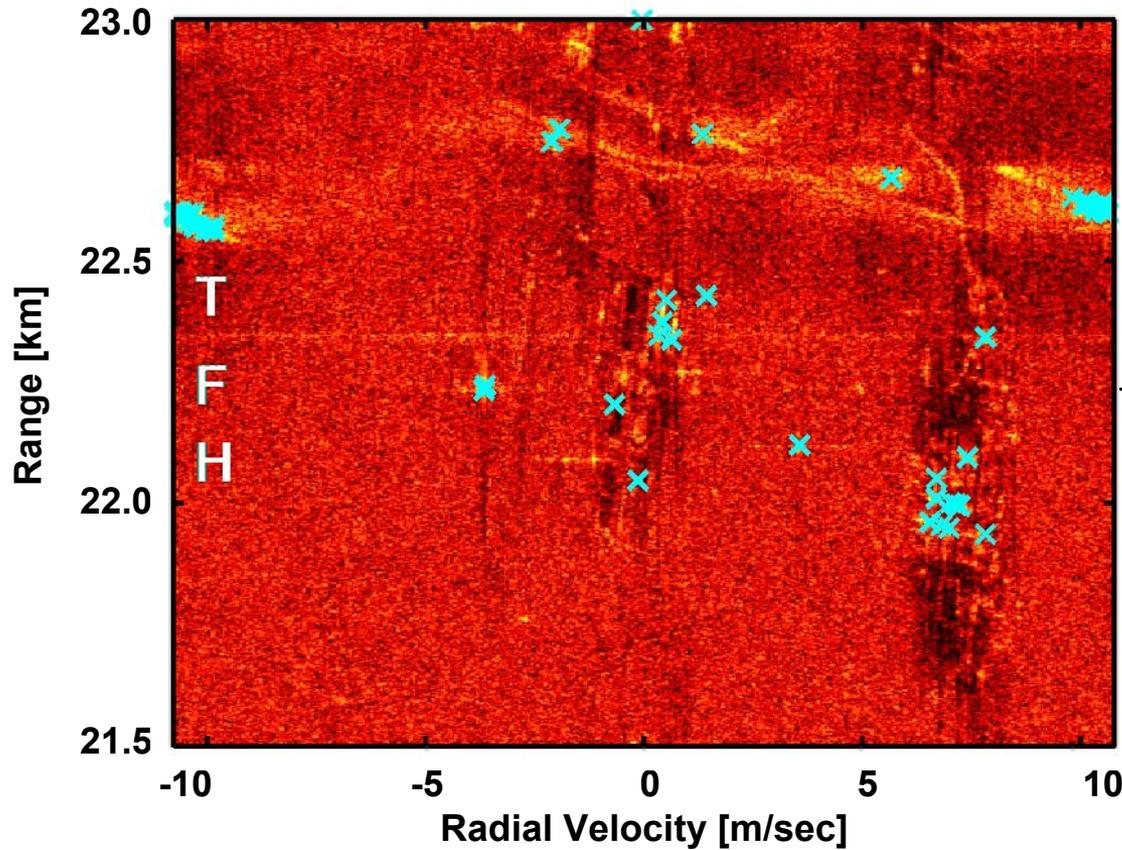


### System Parameters for GMTI Mode

Center Freq.	9.6 GHz
Bandwidth	66 MHz
PRF	1,400 Hz
Tx Apertures	1
Rx Apertures	3
Az BW, Aperture	3.6 deg
EI BW, Aperture	9.1 deg
Polarization	HH
A/C Heading	290 deg
Depr. Angle	15 deg
Recorded Time	40-60 sec



# Example GMTI Output with Tuxedo Data



T = 2-ton Truck  
F = Fuel Truck  
H = HMMWV

× = Target Detection

## BASELINE GMTI PROCESSING STREAM

Adaptive Beamform

Pulse Compression

Doppler Filter

STAP

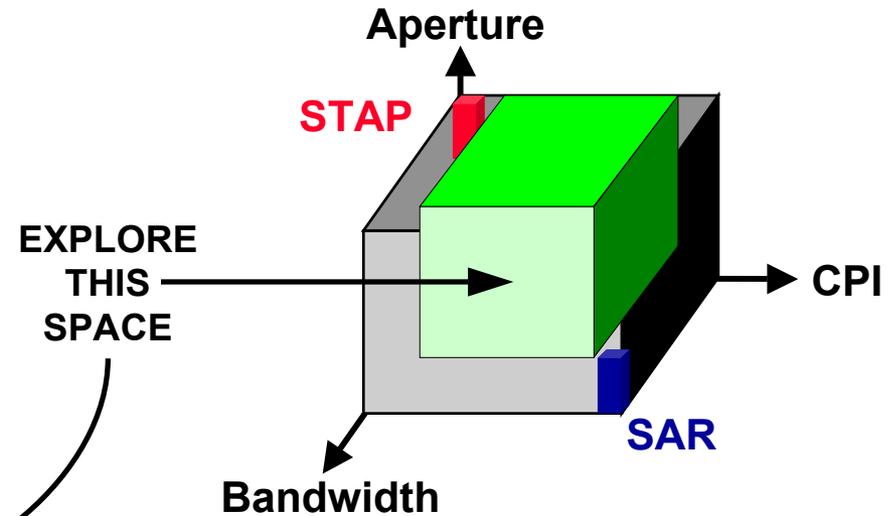
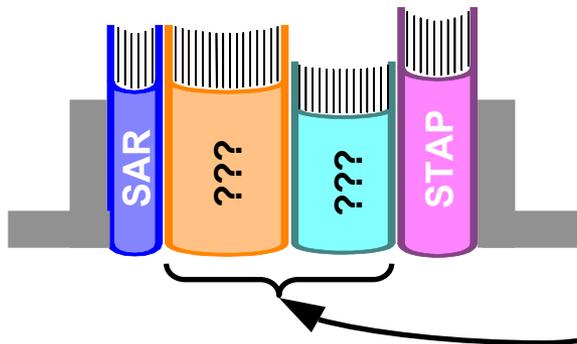
CFAR Detection



# Lincoln Laboratory Goals in the KASSPER Program



- Develop signal processing architecture and algorithms that exploit a priori knowledge to overcome ISR challenges and improve performance
  - Moving Target Focusing
  - Multi-channel adaptive SAR
  - Power Variable Training
  - Extended Array Receiver

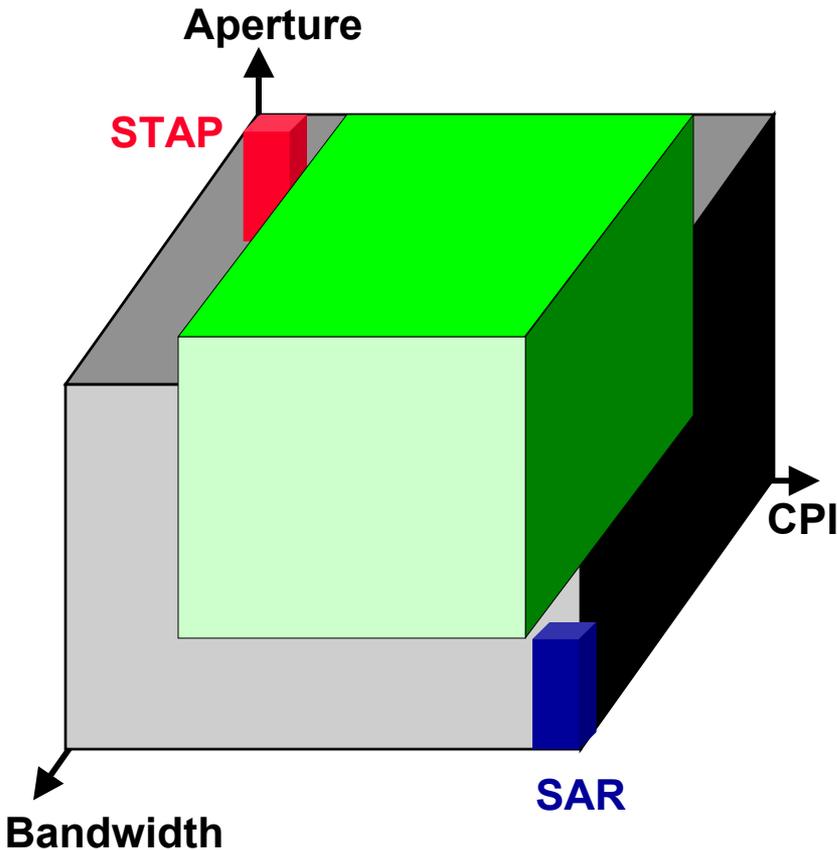


- Develop new High Performance Embedded Computing (HPEC) architecture for real-time Intelligence, Surveillance, and Reconnaissance (ISR) applications
- Real-time flight demonstrations





# SAR versus STAP Processing\*



\*Slide courtesy of Jen Jao

- **STAP adaptively nulls clutter and jammers to achieve noise-limited detection**
  - Fast target revisit, high area search rate
  - Long aperture for low MDV
- **High-resolution SAR employs long CPIs and high bandwidth to enhance target gain and reduce clutter strength**
  - Clutter-limited detection
  - Slow target revisit, low area search rate
- **Aperture size, CPI length and bandwidth may be selected to optimize MDV performance**
- **Adaptive array processing over long CPIs and large bandwidth needs to address**
  - Spatial clutter heterogeneity
  - Clutter training sample support
  - Target migration



# Outline



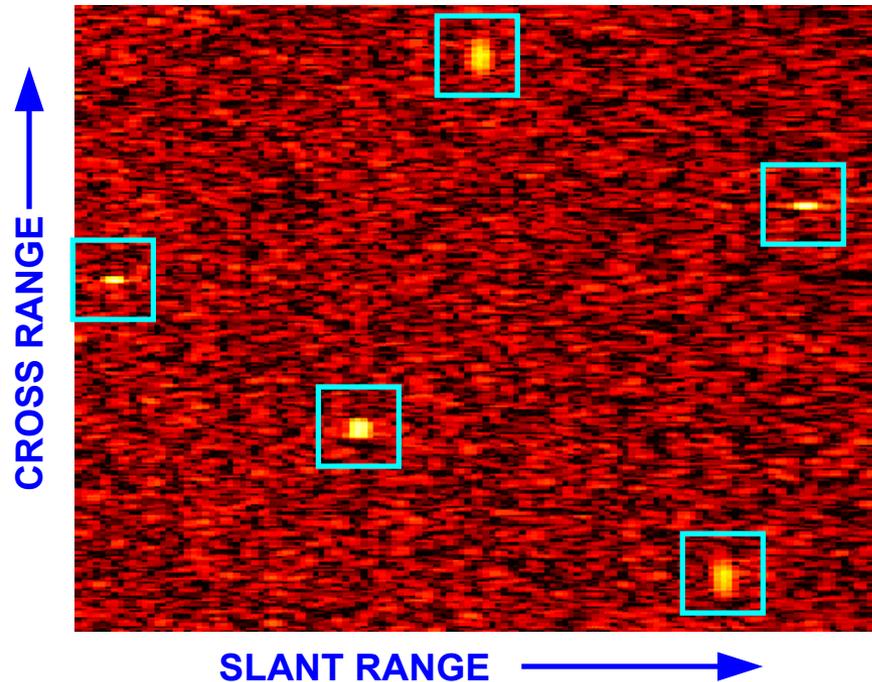
- Introduction
- New Concepts for GMTI Performance Improvements
  - **– Moving Target Focusing**
  - Power Variable Training
  - Multi channel Adaptive SAR
  - Extended Array Receiver
- Summary



# Defocus of Moving Targets with Cross-Range Motion



SIMULATED SAR IMAGE FOCUSED FOR STATIONARY TARGETS



STATIONARY CLUTTER

MOVING TARGETS WITH CROSS-RANGE MOTION

- Targets moving in slant-range dimension will appear displaced in cross-range relative to stationary clutter
- Targets moving in cross-range dimension will appear smeared in doppler or cross-range

EXPLORED  
HERE



# Mechanism for Moving Target Smearing



Significant range walk with large  $BW$  and  $T$

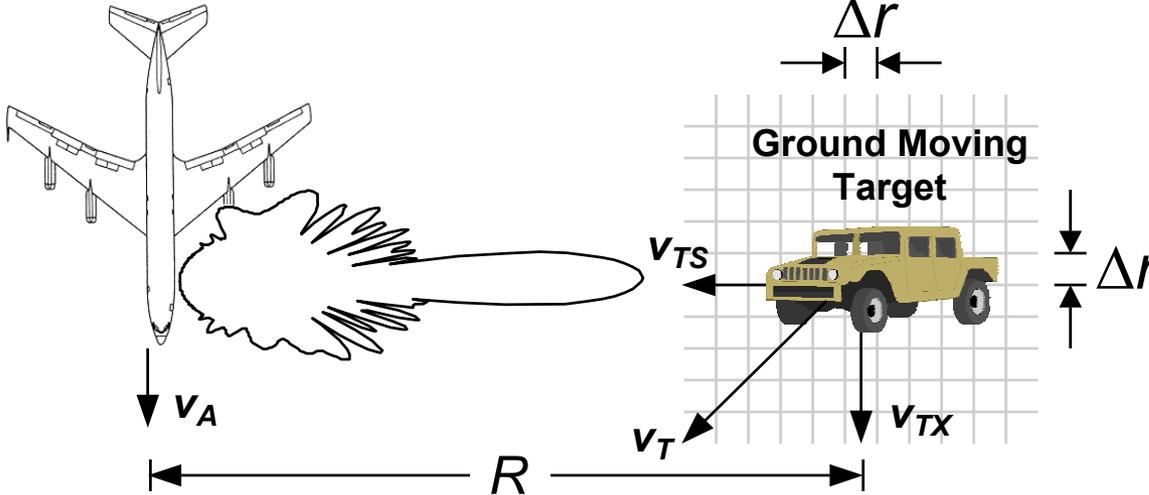
$$\Delta r = \frac{1.81}{BW} \left( \frac{c}{2} \right)$$

Significant doppler walk with large  $T$

$$\Delta \dot{r} = \frac{1.81}{T} \left( \frac{\lambda}{2} \right)$$

- $c$  Speed of Light
- $BW$  Bandwidth
- $\lambda$  Wavelength
- $T$  CPI Time
- $v_A$  Aircraft Velocity
- $v_T$  Target Velocity
- $R$  Stand-off Range

Airborne Radar Platform



$$\gamma^2 \equiv (v_A - v_{TX})^2 + v_{TS}^2$$

$$r(t) = \sqrt{R^2 + 2Rv_{TS}t + \gamma^2 t^2}$$

$$\dot{r}(t) = (Rv_{TS} + \gamma^2 t) / r(t)$$

Long CPIs can lead to target doppler walk or smearing.  
The degree of smearing is a function of  $\gamma^2$



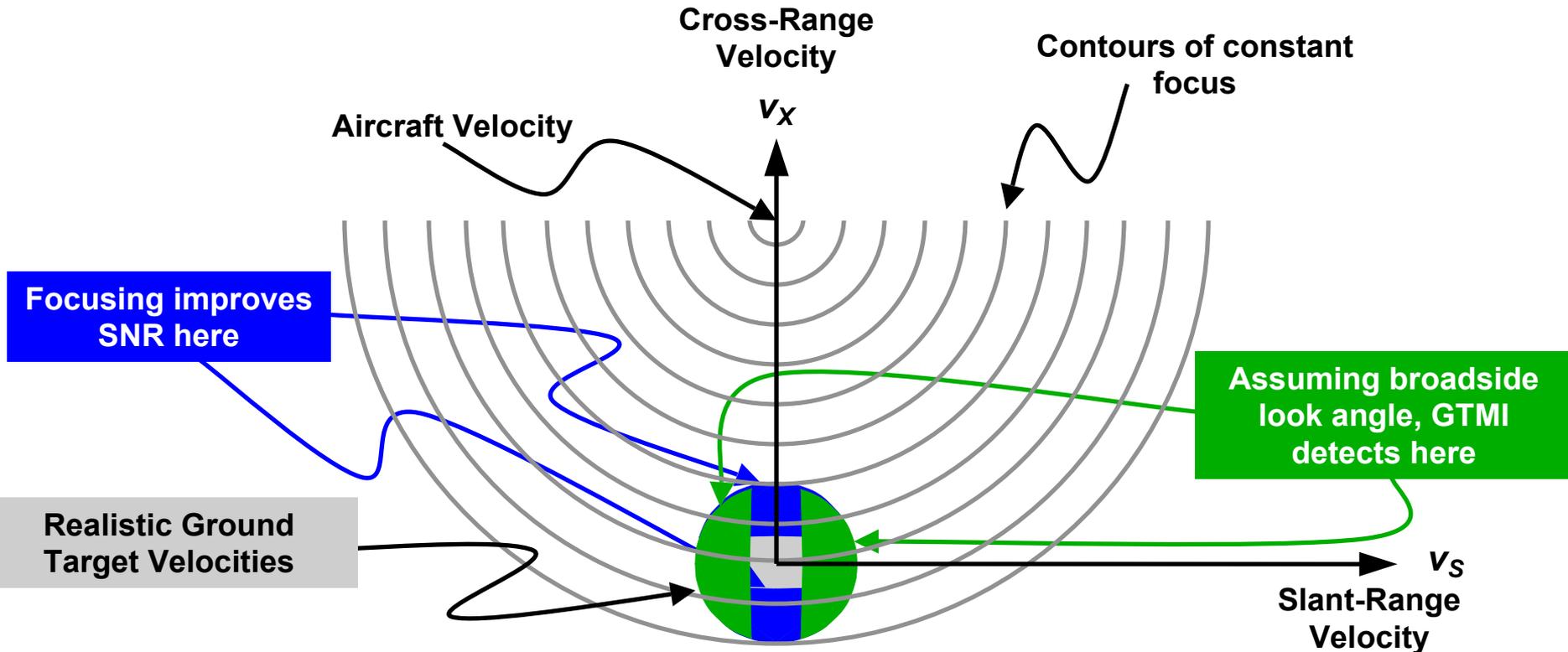
# Defocusing Factor



Defocusing Factor

$$\gamma \equiv \sqrt{(V_A - V_{TX})^2 + V_{TS}^2}$$

Norm of the relative velocity vector



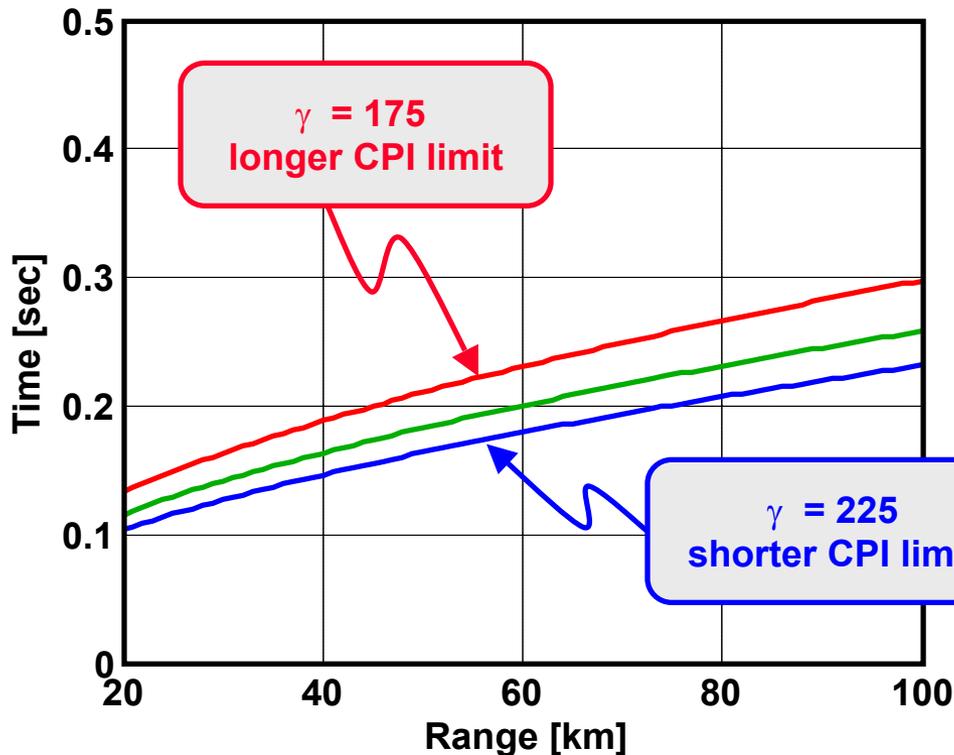
Focus of moving targets is parameterized with a single scalar quantity



# Limits on CPI Time to Prevent Doppler-walk



$$\dot{r}(T/2) - \dot{r}(-T/2) \leq \frac{1.81}{T} \left( \frac{\lambda}{2} \right) \quad \text{Assume large } R \quad \longrightarrow \quad T \leq \sqrt{\frac{1.81 R \lambda}{\gamma^2 2}}$$



- Center Frequency 10 GHz
- Platform Velocity 200 m/sec
- Target at broadside
- DFT with Hamming weighting

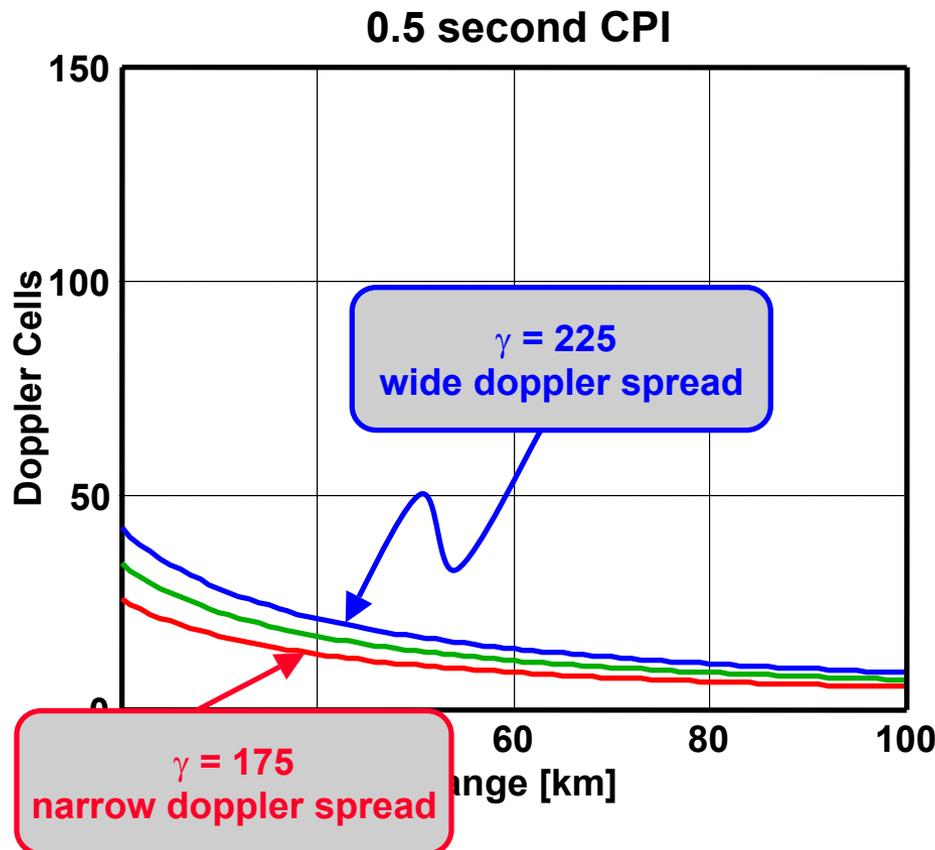
Velocities in m/sec		
	$V_x$	$\gamma$
— (Red)	25	175
— (Green)	0	200
— (Blue)	-25	225



# Moving Target Doppler Spread



$$\frac{\dot{r}(T/2) - \dot{r}(-T/2)}{\Delta \dot{r}} \approx \frac{2\gamma^2 T^2}{\lambda R} \quad \text{Assume large } R$$



- Center Frequency 10 GHz
- Platform Velocity 200 m/sec
- Target at broadside
- DFT with Hamming weighting

Velocities in m/sec		
	$V_x$	$\gamma$
— (red)	25	175
— (green)	0	200
— (blue)	-25	225



# GMTI Focusing



$$\begin{aligned} \dot{r}(t) &= (Rv_{TS} + \gamma^2 t) / r(t) \\ &\approx (Rv_{TS} + \gamma^2 t) / R \\ &\approx v_{TS} + \gamma^2 t / R \end{aligned}$$

Constant term

Term Affecting Defocus

Moving Target Defocuses with:

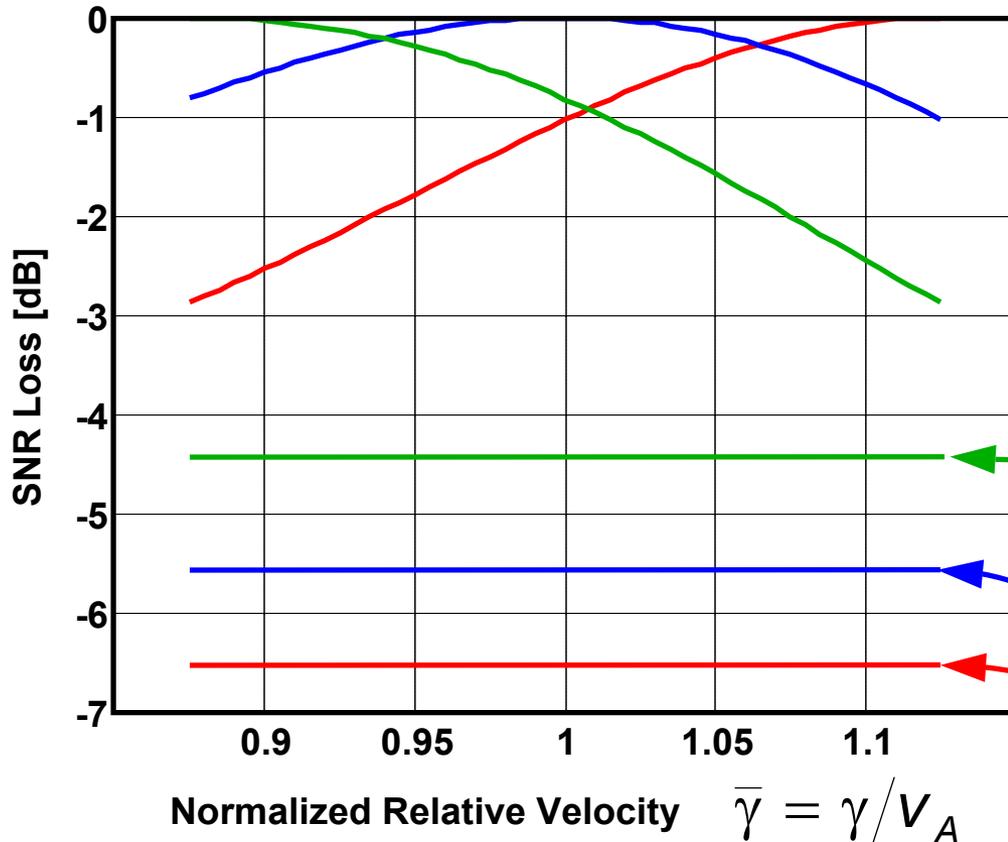
- Increasing CPI time
- Increasing  $\gamma$
- Decreasing range

$$\exp\left[\frac{j2\pi\gamma^2 t^2}{\lambda R}\right]$$

Correcting for target motion consists of applying a quadratic phase term to each pulse



# Sensitivity to $\gamma$



- 10 GHz Center Frequency
- Platform Velocity 200 m/sec
- 0.5 second integration time
- 60 km slant range

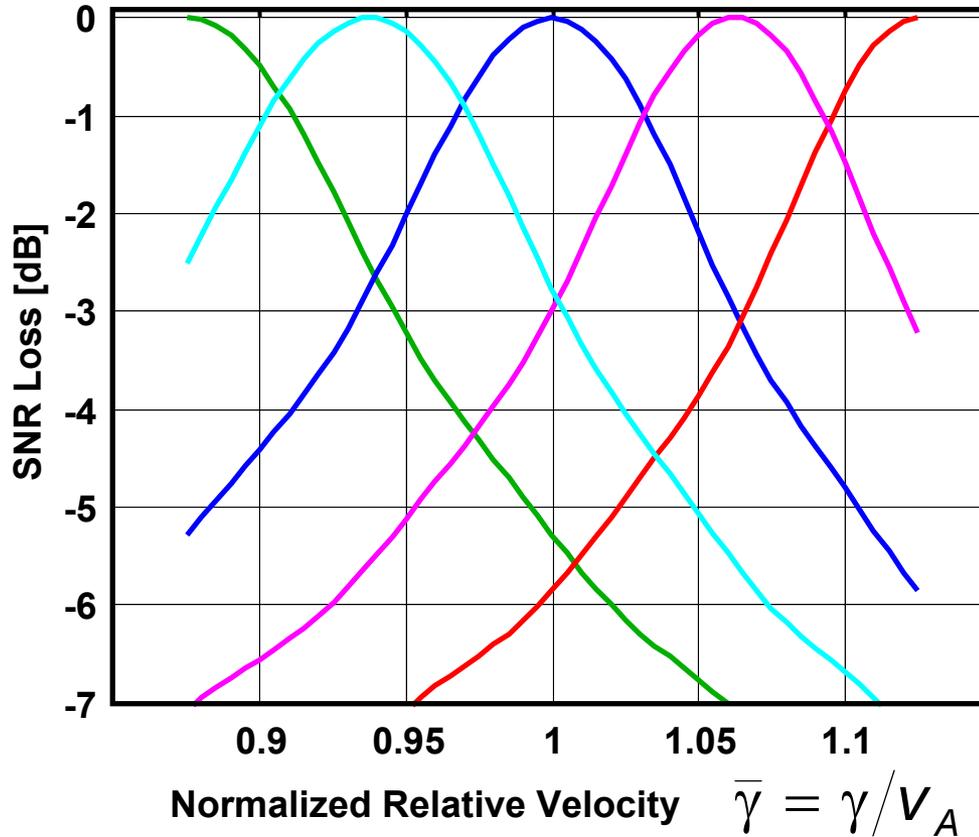
Velocities in m/sec		
	$V_x$	$\gamma$
Red line	25	175
Green line	0	200
Blue line	-25	225

SNR Loss without focusing,  
assume usual FFT Doppler  
processing ( set  $\gamma = 0$  )

**A bank of focusing filters (for different values of  $\gamma$ ) is required.  
Analogous to Doppler filterbank architecture**



# Sensitivity to $\gamma$



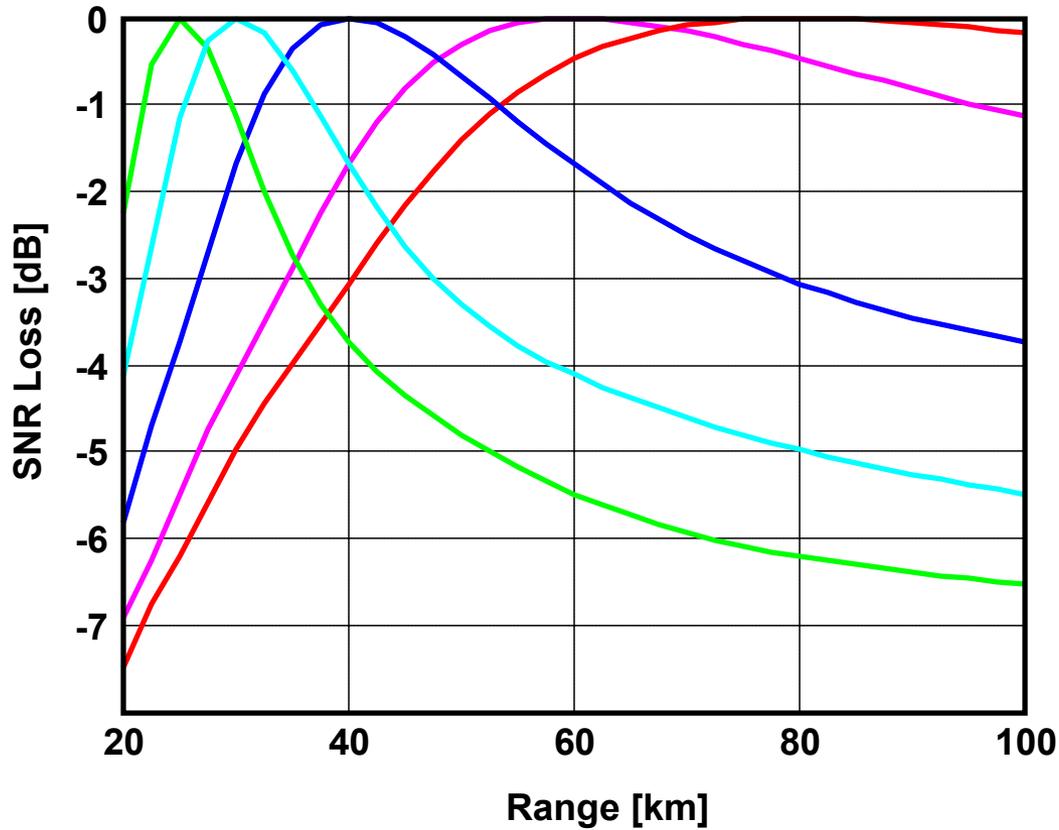
- 10 GHz Center Frequency
- Platform Velocity 200 m/sec
- 1.0 second integration time
- 60 km slant range

Velocities in m/sec		
	$V_x$	$\gamma$
—	25.0	175
—	12.5	189
—	0.0	200
—	-12.5	214
—	-25.0	225

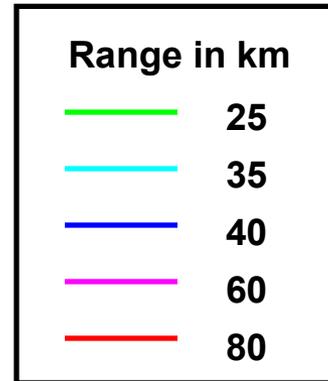
With longer integration times, more filters are required.



# Sensitivity to Range



- 10 GHz Center Frequency
- 0.5 second integration time
- 200 m/sec platform velocity
- 25 m/sec target velocity



Phase correction may vary over long range swaths

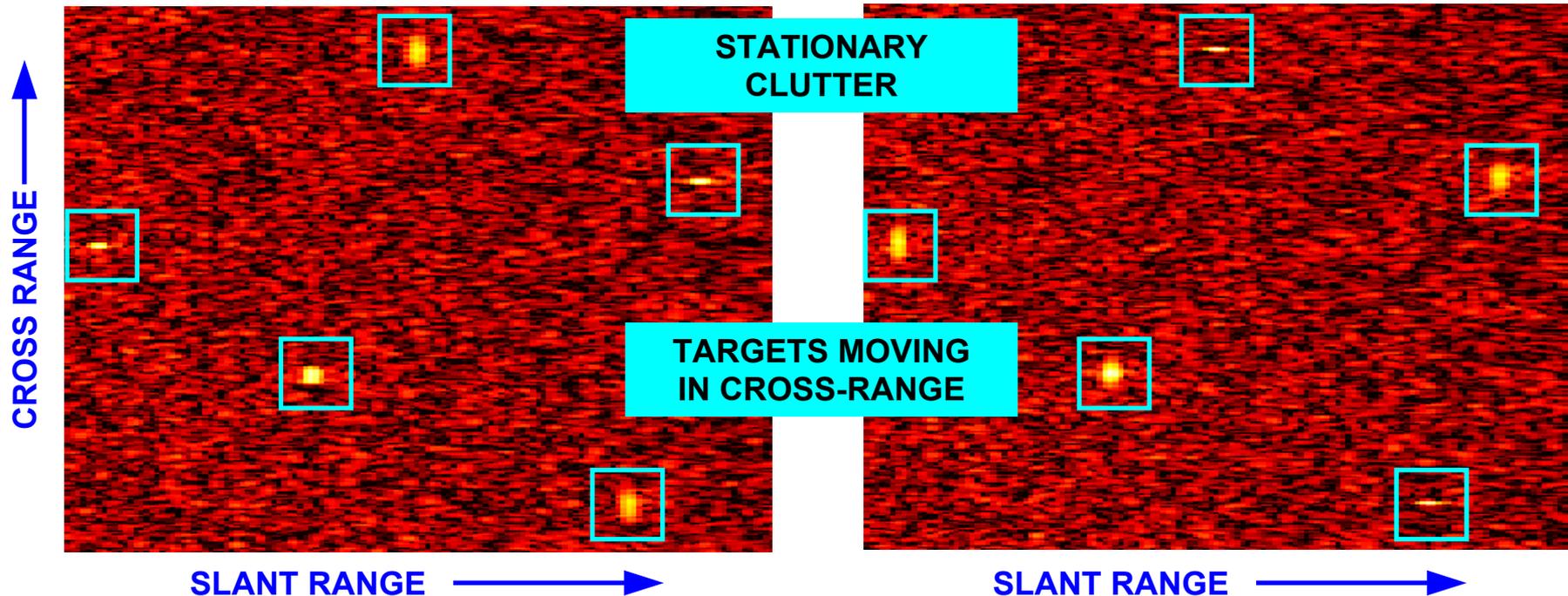


# Moving Target focusing for Targets with Transverse Motion



**SIMULATED SAR IMAGE FOCUSED FOR STATIONARY TARGETS**

**SIMULATED SAR IMAGE FOCUSED FOR MOVING TARGETS**



- Targets moving in cross range will appear smeared in a traditional SAR image and will “cohere-up” in a SAR image focused for moving targets
- If cross range motion is significant over integration time then comparing the two SAR images can separate moving targets from clutter (stationary targets)

REFERENCE J. Jao, “Theory of synthetic aperture radar imaging of a moving target,” IEEE Trans. on Geoscience and Remote Sensing, 2001.



# Outline



- Introduction
- New Concepts for GMTI Performance Improvements
  - Moving Target Focusing
  - **Power Variable Training**
  - Multi channel Adaptive SAR
  - Extended Array Receiver
- Summary

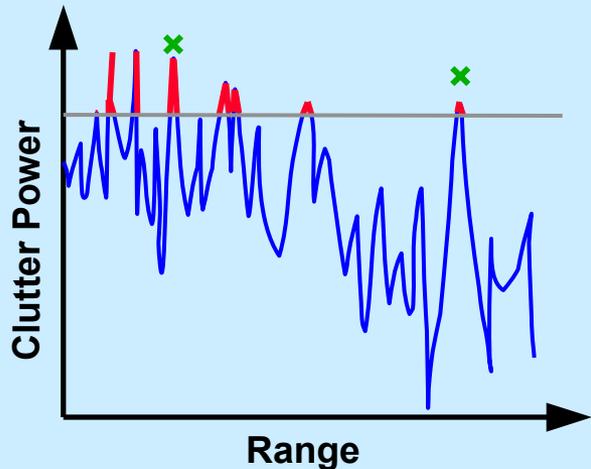




# Power-Variable Training (Without Overnulling)

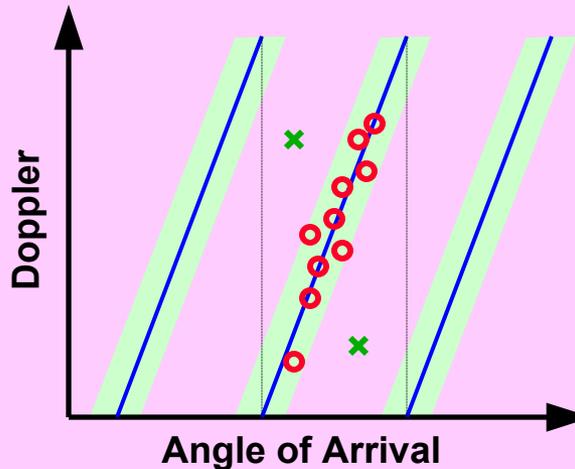


## POWER SELECTIVE TRAINING



Select strongest clutter returns as candidate training samples

## EXCISION



Excise samples away from clutter ridge (potential targets)

## ESTIMATION

$$\mathbf{R}_M = \beta \left( \frac{1}{K} \sum \mathbf{x}_i \mathbf{x}_i^H \right) + \lambda \mathbf{I}$$

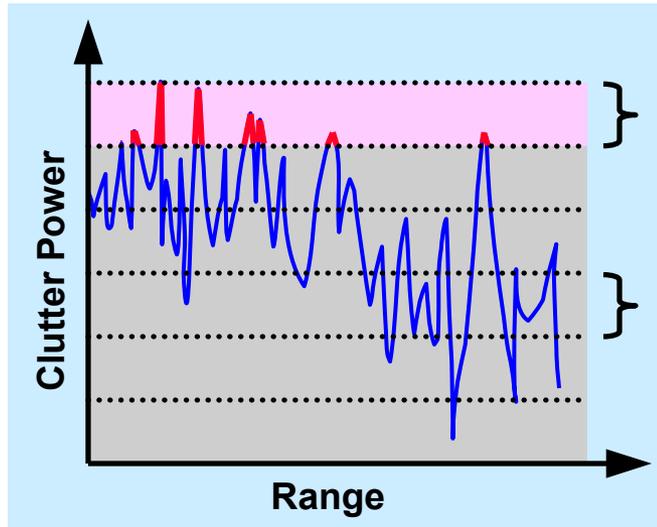
$$\beta < 1$$

Scale training samples to estimated CNR

- Power scaling provides lower MDV than power selective training
- Power scaling may generate more false alarms relative to power selective training but adaptive sidelobe blanking should remove most of them



# Power Variable Training Procedure



Training

Tile "M"

$$\mathbf{R}_L = \frac{1}{K_L} \sum x_i x_i^H$$

$$e_M = \frac{1}{K_M} \sum x_i^H x_i$$

Estimate Pure Clutter  
Covariance Matrix

$$\mathbf{R}_C = \mathbf{R}_L - \lambda \mathbf{I}$$

$\lambda =$  Estimated  
Noise Floor

Covariance Matrix  
for Tile "M"

$$\mathbf{R}_M = \beta \mathbf{R}_C + \lambda \mathbf{I}$$

$$\beta = \frac{e_M - N\lambda}{\text{tr}[\mathbf{R}_L] - N\lambda}$$

Adaptive Weight  
for Tile "M"

$$w_M = \frac{[\mathbf{R}_M + \delta \mathbf{I}]^{-1} v}{\sqrt{v^H [\mathbf{R}_M + \delta \mathbf{I}]^{-1} v}}$$

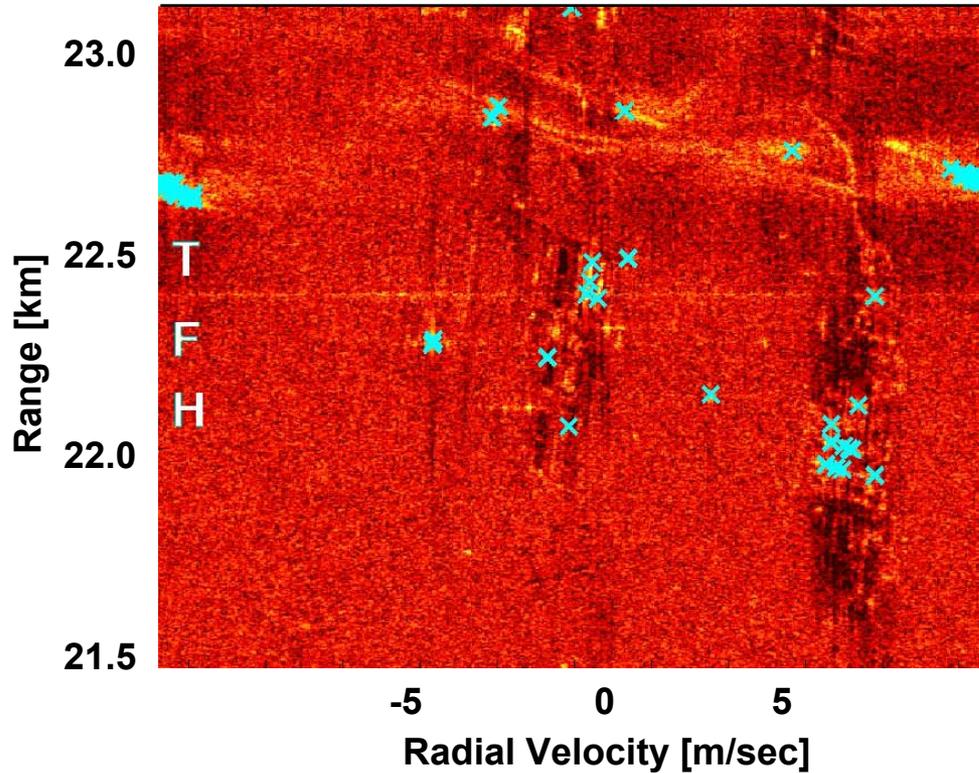
$\delta =$  Diagonal  
Load Level



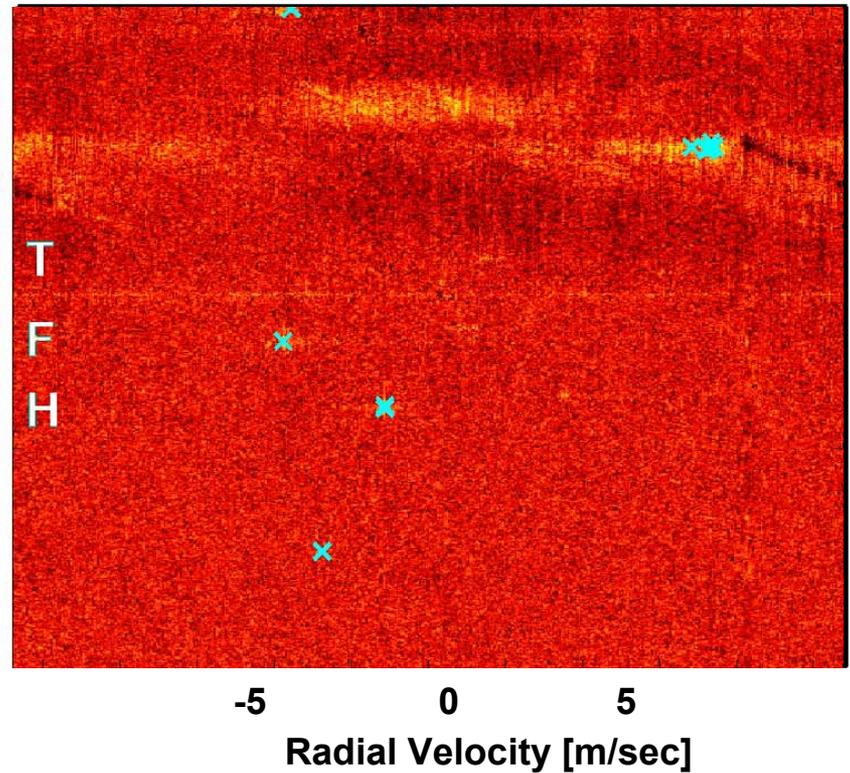
# Example with Tuxedo Data



## Baseline STAP



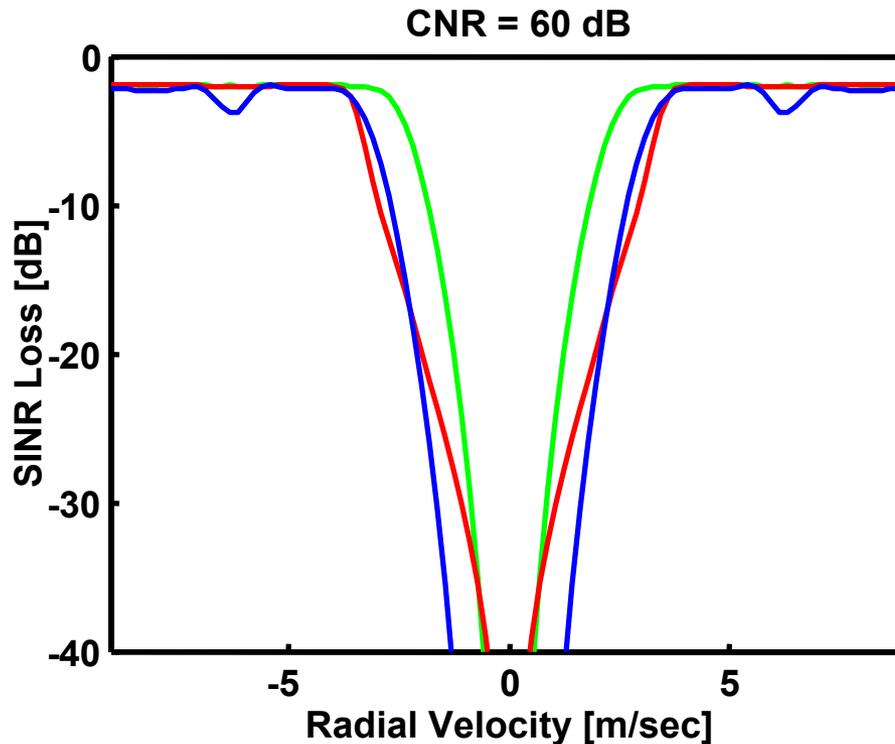
## Power Variable Training



**Power Variable Training SIGNIFICANTLY improves false alarm performance relative to baseline STAP approach**



# Overnulling / Undernulling Performance



## PARAMETERS

Aperture	4 m
Channels	7
Center Freq.	10 GHz
PRF	1.2 kHz
Sample Rate	20 MHz
Pulses	34
A/C Velocity	200 m/sec

- Matched
- 30 dB Undernulling
- 30 dB Overnulling

**Matching CNR avoids unnecessary SINR Losses due to overnulling or undernulling**



# Outline

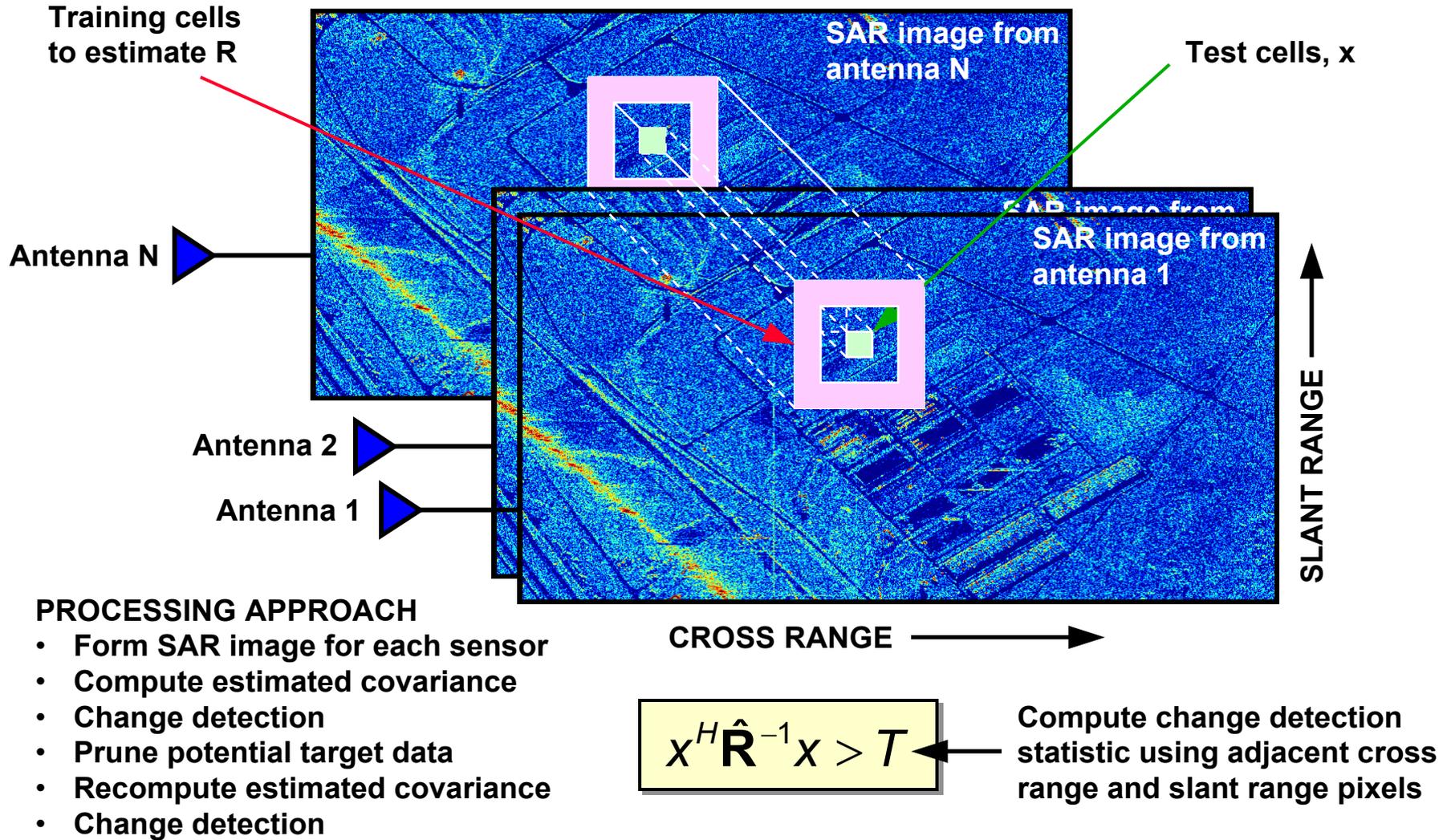


- Introduction
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  - Extended Array Receiver
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# Multi-Channel Adaptive SAR



REFERENCE A. Yegulalp, *FOPEN GMTI Using Multi-Channel Adaptive SAR*, Proceedings of the ASAP Workshop, March 2002.



# Open Issues with Multi-Channel Adaptive SAR Processing

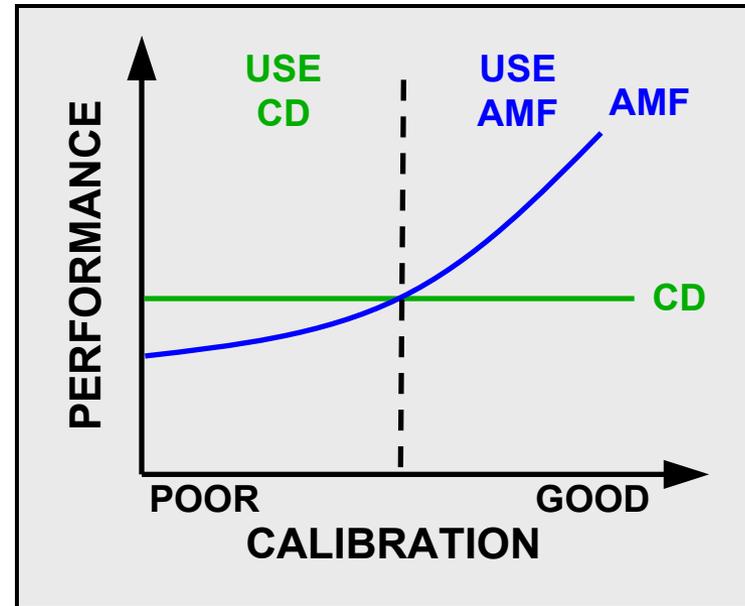


CD TEST

$$x^H \hat{\mathbf{R}}^{-1} x > T$$

AMF TEST

$$\frac{|v^H \hat{\mathbf{R}}^{-1} x|^2}{v^H \hat{\mathbf{R}}^{-1} v} > T$$



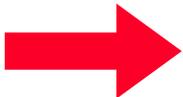
- For well calibrated arrays the adaptive matched filter (AMF) approach outperforms the change detection (CD) approach
- For what amount of array uncertainty does the change detection approach become more useful?
- Do we need to generate focused SAR images for each antenna element or will simple Doppler processing suffice?



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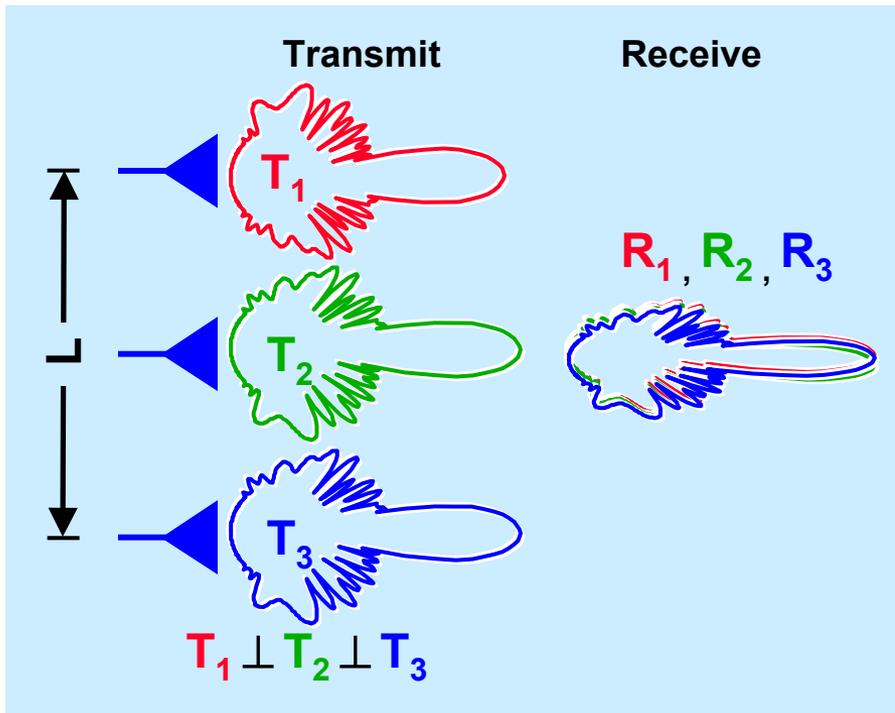




# Extended Array Receiver



## SYSTEM CONCEPT



- Transmit orthogonal waveforms on each subarray
- Receive and demodulate each waveform across the entire array
- This approach transfers the available transmit gain of the full aperture to the receiver, providing flexibility
- Note, some antenna systems spoil the gain on transmit for wider coverage

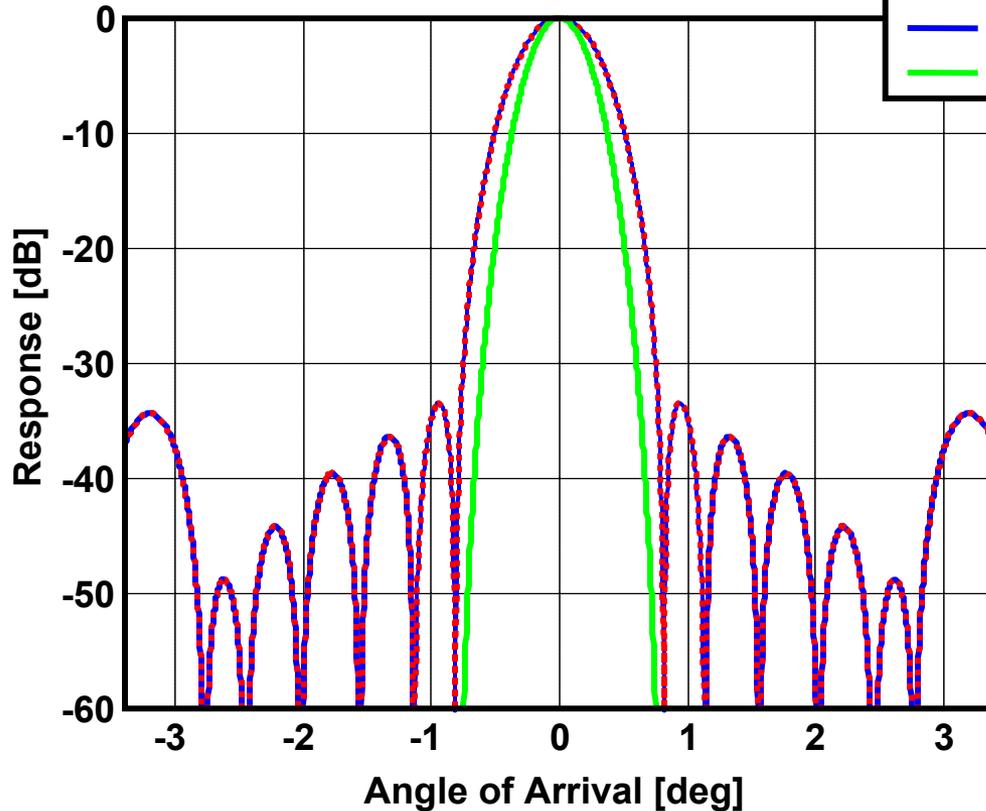
Provides narrow transmit-receive beampatterns  
over wide coverage area



# Theoretical Transmit-Receive Beampatterns

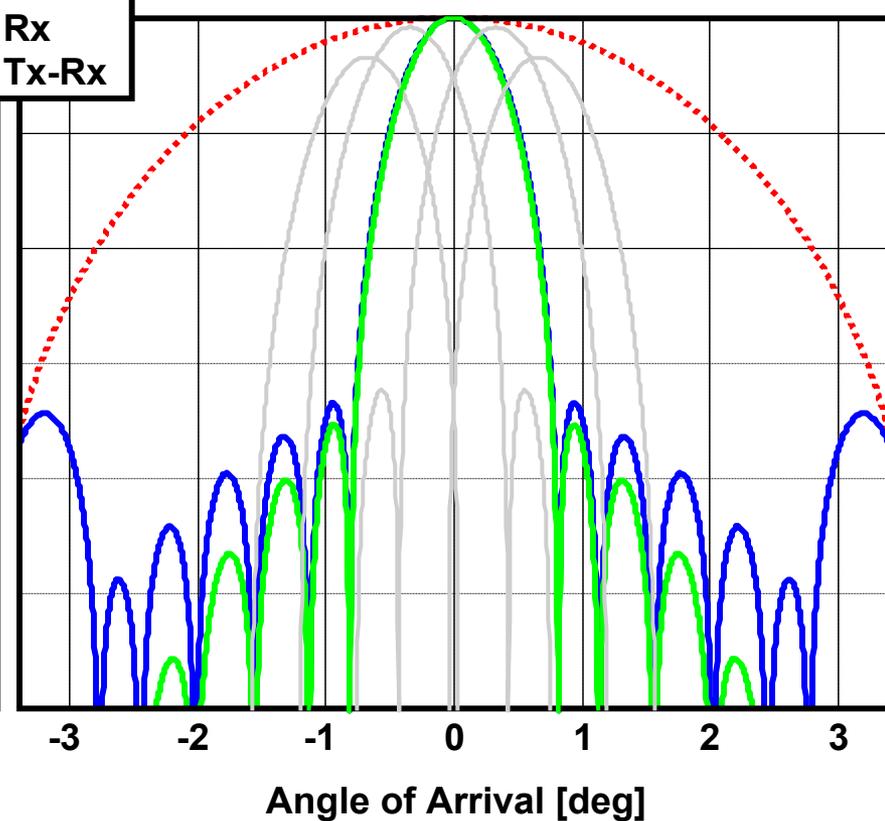


Full-Aperture on Transmit  
Full-Aperture on Receive



**Narrow two-way beampatterns**  
**Small coverage area**

Sub-Aperture on Transmit  
Full-Aperture on Receive



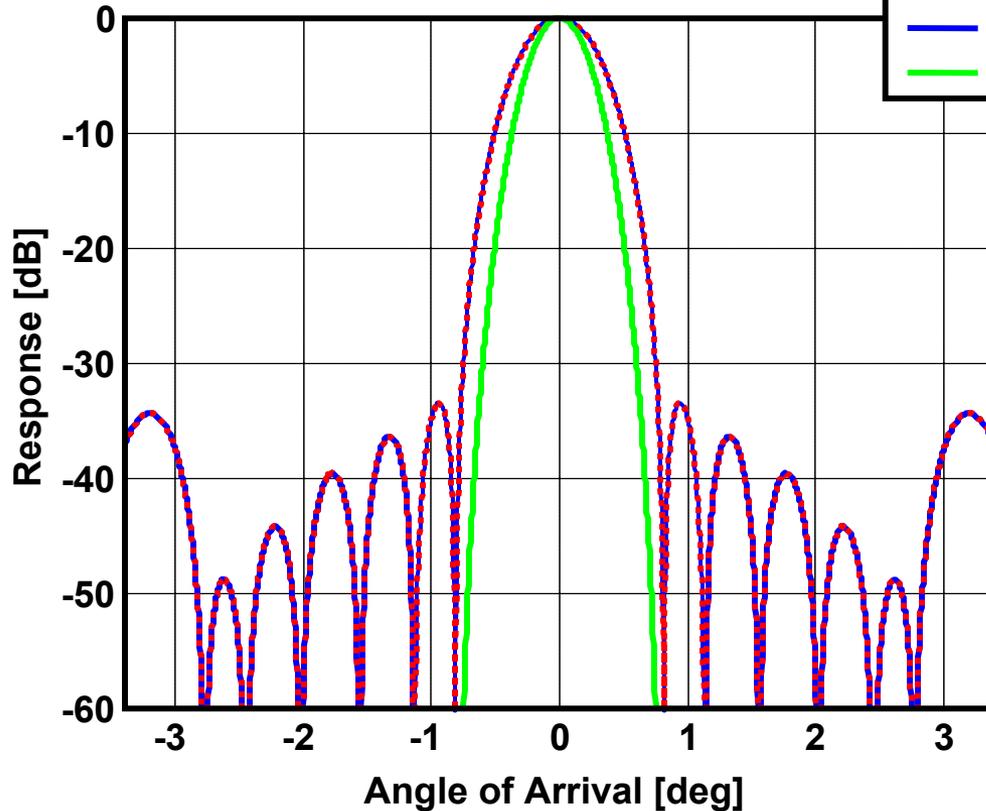
**Wide two-way beampatterns**  
**Large coverage area**



# Theoretical Transmit-Receive Beampatterns

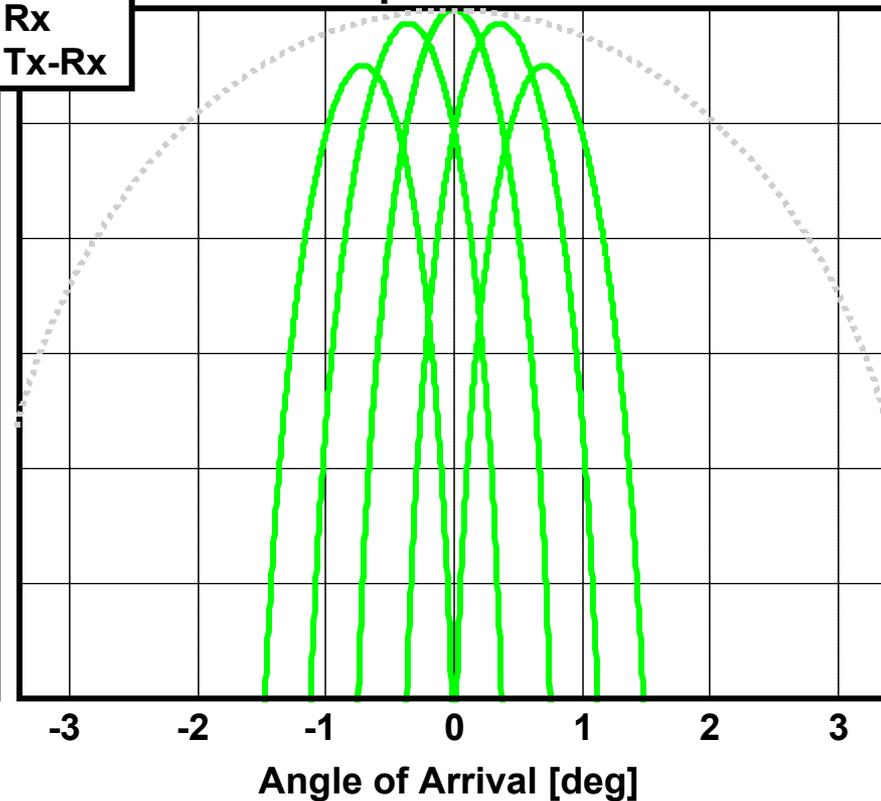


Full-Aperture on Transmit  
Full-Aperture on Receive



Narrow two-way beampatterns  
Small coverage area

Sub-Aperture on Transmit with  
orthogonal waveforms  
Extended Aperture on Receive



Narrow two-way beampatterns  
Large coverage area



# Open Issues with Extended Array Receiver Concept



- **Elevated receiver noise floor with multiple orthogonal waveforms**
- **Can a processor architecture support multiple orthogonal waveform decoding per subarray?**
- **How nearly orthogonal can multiple waveforms be over both delay and doppler?**
- **In some cases internal clutter motion may limit the benefit of an extended array receiver**
- **Need to investigate synchronization of orthogonal waveforms on reception**



# Summary of GMTI Performance Improvements



	Moving Target Focusing	Multi-channel Adaptive SAR	Power Variable Training	Training Data Excision	Extended Array Receiver
Controls False Alarms	Green	White	Green	White	White
Improves MDV	Green	Green	Green	White	Green
Heterogeneous Clutter	White	Green	Green	White	White
Avoids Target Self-nulling	White	Green	White	Green	White



# Summary



- **GMTI is challenging in real-world applications**
  - Excessive false alarms
  - Missed Detections (slow moving vehicles)
  - Dense target scenarios
  - Heterogeneous clutter environments
- **Explored several approaches to improve GMTI performance**
  - Moving target focusing for long CPIs
  - Excision of training data far from clutter ridge
  - Power variable training without overnulling
  - Multi-channel adaptive SAR
  - Extended array receiver
- **Developing system-oriented approaches to exploit a priori knowledge with respect to front-end and back-end signal processing and scheduling**
- **Implementation on real-time testbed will be evaluated**
- **Ongoing evaluation with simulated and recorded radar data**